

Generalized b Continuous Mappings in Intuitionistic Fuzzy Topological Spaces

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Abstract— In this paper we have introduced generalized b continuous mappings in Intuitionistic fuzzy topological space and some of their basic properties are studied.

Keywords— Intuitionistic fuzzy topology, Intuitionistic fuzzy generalized b closed sets, Intuitionistic fuzzy generalized b continuous mappings, Intuitionistic fuzzy $bT_{1/2}$ ($IF_bT_{1/2}$) space and Intuitionistic fuzzy $b_gT_{1/2}$ ($IF_{b_g}T_{1/2}$) space.

I. INTRODUCTION

The concept of fuzzy sets was introduced by Zadeh [13] and later Atanassov [1] generalized this idea to Intuitionistic fuzzy sets using the notion of fuzzy sets. On the other hand Coker [4] introduced Intuitionistic fuzzy topological spaces using the notion of Intuitionistic fuzzy sets. In this paper, we introduce Intuitionistic fuzzy generalized b continuous mappings and studied some of their basic properties. We arrive at some characterizations of Intuitionistic fuzzy generalized b continuous mappings.

II. PRELIMINARIES

Definition 2.1: [1] Let X be a non-empty fixed set. An Intuitionistic fuzzy set (IFS in short) A in X is an object having the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$$

where the functions $\mu_A(x): X \rightarrow [0, 1]$ and $\nu_A(x): X \rightarrow [0, 1]$ denote the degree of membership (namely $\mu_A(x)$) and the degree of non-membership (namely $\nu_A(x)$) of each element $x \in X$ to the set A , respectively, and $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ for each $x \in X$. Denote the set of all Intuitionistic fuzzy sets in X by $IFS(X)$.

Definition 2.2: [1] Let A and B be IFSs of the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \} \text{ and } B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle / x \in X \}.$$

(a) $A \subseteq B$ if and only if $\mu_A(x) \leq \mu_B(x)$ and $\nu_A(x) \geq \nu_B(x)$ for all $x \in X$

(b) $A = B$ if and only if $A \subseteq B$ and $B \subseteq A$

$$(c) A^c = \{ \langle x, \nu_A(x), \mu_A(x) \rangle / x \in X \}$$

$$(d) A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle / x \in X \}$$

$$(e) A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle / x \in X \}$$

For the sake of simplicity, we shall use the notation $A = \langle x, \mu_A, \nu_A \rangle$ instead of $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$. Also for the sake of simplicity, we shall use the notation $A = \langle x, (\mu_A, \mu_B), (\nu_A, \nu_B) \rangle$ instead of $A = \langle x, (A/\mu_A, B/\mu_B), (A/\nu_A, B/\nu_B) \rangle$.

The Intuitionistic fuzzy sets $0_\sim = \{ \langle x, 0, 1 \rangle / x \in X \}$ and $1_\sim = \{ \langle x, 1, 0 \rangle / x \in X \}$ are respectively the empty set and the whole set of X .

Definition 2.3: [3] An Intuitionistic fuzzy topology (IFT in short) on X is a family τ of IFSs in X satisfying the following axioms.

- (i) $0_\sim, 1_\sim \in \tau$
- (ii) $G_1 \cap G_2 \in \tau$ for any $G_1, G_2 \in \tau$
- (iii) $\cup G_i \in \tau$ for any family $\{ G_i / i \in J \} \subseteq \tau$.

In this case the pair (X, τ) is called an Intuitionistic fuzzy topological space (IFTS in short) and any IFS in τ is known as an Intuitionistic fuzzy open set (IFOS in short) in X .

The complement A^c of an IFOS A in IFTS (X, τ) is called an Intuitionistic fuzzy closed set (IFCS in short) in X .

Definition 2.4: [3] Let (X, τ) be an IFTS and $A = \langle x, \mu_A, \nu_A \rangle$ be an IFS in X . Then the Intuitionistic fuzzy interior and Intuitionistic fuzzy closure are defined by

$$\text{int}(A) = \cup \{ G / G \text{ is an IFOS in } X \text{ and } G \subseteq A \},$$

$$\text{cl}(A) = \cap \{ K / K \text{ is an IFCS in } X \text{ and } A \subseteq K \}.$$

Note that for any IFS A in (X, τ) , we have $\text{cl}(A^c) = [\text{int}(A)]^c$ and $\text{int}(A^c) = [\text{cl}(A)]^c$.

Definition 2.5: [7] An IFS $A = \langle x, \mu_A, \nu_A \rangle$ in an IFTS (X, τ) is said to be an

- (i) Intuitionistic fuzzy semi open set (IFSOS in short) if $A \subseteq \text{cl}(\text{int}(A))$,
- (ii) Intuitionistic fuzzy α -open set ($IF\alpha OS$ in short) if $A \subseteq \text{int}(\text{cl}(\text{int}(A)))$,
- (iii) Intuitionistic fuzzy regular open set (IFROS in short) if $A = \text{int}(\text{cl}(A))$.

The family of all IFOS (respectively IFSOS, $IF\alpha OS$, IFROS) of an IFTS (X, τ) is denoted by $IFO(X)$ (respectively $IFSOS(X)$, $IF\alpha O(X)$, $IFRO(X)$).

Definition 2.6: [7] An IFS $A = \langle x, \mu_A, \nu_A \rangle$ in an IFTS (X, τ) is said to be an

- (i) Intuitionistic fuzzy semi closed set (IFSCS in short) if $\text{int}(\text{cl}(A)) \subseteq A$,
- (ii) Intuitionistic fuzzy α -closed set ($IF\alpha CS$ in short) if $\text{cl}(\text{int}(\text{cl}(A))) \subseteq A$,

(iii) Intuitionistic fuzzy regular closed set (IFRCS in short) if $A = \text{cl}(\text{int}(A))$.

The family of all IFCS (respectively IFSCS, $\text{IF}\alpha\text{CS}$, IFRCS) of an IFTS (X, τ) is denoted by $\text{IFC}(X)$ (respectively $\text{IFSC}(X)$, $\text{IF}\alpha\text{C}(X)$, $\text{IFRC}(X)$).

Definition 2.7: [8] Let A be an IFS in an IFTS (X, τ) . Then $\text{bint}(A) = \cup \{ G / G \text{ is an IFbOS in } X \text{ and } G \subseteq A \}$, $\text{bcl}(A) = \cap \{ K / K \text{ is an IFbCS in } X \text{ and } A \subseteq K \}$.

Note that for any IFS A in (X, τ) , we have $\text{scl}(A^c) = (\text{sint}(A))^c$ and $\text{sint}(A^c) = (\text{scl}(A))^c$.

Definition 2.8: [11] An IFS A in an IFTS (X, τ) is an (i) Intuitionistic fuzzy generalized closed set (IFGCS in short) if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IFOS in X . (ii) Intuitionistic fuzzy regular generalized closed set (IFRGCS in short) if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IFROS in X .

Definition 2.9: [10] An IFS A in an IFTS (X, τ) is said to be an Intuitionistic fuzzy generalized semi closed set (IFGSCS in short) if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IFOS in (X, τ) .

Definition 2.10: [10] An IFS A is said to be an Intuitionistic fuzzy generalized semi open set (IFGSOS in short) in X if the complement A^c is an IFGSCS in X .

The family of all IFGSCSs (IFGSOSs) of an IFTS (X, τ) is denoted by $\text{IFGSC}(X)$ ($\text{IFGSO}(X)$).

Definition 2.11: [8] An IFS A in an IFTS (X, τ) is said to be an Intuitionistic fuzzy π -generalized semi closed set ($\text{IF}\pi\text{GSCS}$ in short) if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an $\text{IF}\pi\text{OS}$ in (X, τ) .

Result 2.12: [8] Every IFCS, IFGCS, IFRCS, $\text{IF}\alpha\text{CS}$, IFGSCS is an $\text{IF}\pi\text{GSCS}$ but the converses may not be true in general. Every $\text{IF}\alpha\text{GCS}$ is IFGSCS but the converse is need not be true.

Definition 2.13: [9] An IFS A is said to be an Intuitionistic fuzzy alpha generalized open set ($\text{IF}\alpha\text{GOS}$ in short) in X if the complement A^c is an $\text{IF}\alpha\text{GCS}$ in X .

The family of all $\text{IF}\alpha\text{GCS}$ s ($\text{IF}\alpha\text{GOS}$ s) of an IFTS (X, τ) is denoted by $\text{IF}\alpha\text{GC}(X)$ ($\text{IF}\alpha\text{GO}(X)$).

Definition 2.14: [5] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be Intuitionistic fuzzy continuous (IF continuous in short) if $f^{-1}(B) \in \text{IFO}(X)$ for every $B \in \sigma$.

Definition 2.15: [7] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be

- (i) Intuitionistic fuzzy semi continuous (IFS continuous in short) if $f^{-1}(B) \in \text{IFSO}(X)$ for every $B \in \sigma$.
- (ii) Intuitionistic fuzzy α -continuous ($\text{IF}\alpha$ continuous in short) if $f^{-1}(B) \in \text{IF}\alpha\text{O}(X)$ for every $B \in \sigma$.
- (iii) Intuitionistic fuzzy pre continuous (IFP continuous in short) if $f^{-1}(B) \in \text{IFPO}(X)$ for every $B \in \sigma$.

Result 2.16: [7] Every IF continuous mapping is an $\text{IF}\alpha$ -continuous mapping and every $\text{IF}\alpha$ -continuous mapping is an IFS continuous mapping.

Definition 2.17: [6] A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an Intuitionistic fuzzy γ continuous ($\text{IF}\gamma$ continuous in short) if $f^{-1}(B)$ is an $\text{IF}\gamma\text{OS}$ in (X, τ) for every $B \in \sigma$.

Definition 2.18: [10] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an Intuitionistic fuzzy generalized continuous (IFG continuous in short) if $f^{-1}(B) \in \text{IFGCS}(X)$ for every IFCS B in Y .

Result 2.19: [10] Every IF continuous mapping is an IFG continuous mapping.

Definition 2.20: [9] A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an Intuitionistic fuzzy generalized semi continuous (IFGS continuous in short) if $f^{-1}(B)$ is an IFGSCS in (X, τ) for every IFCS B of (Y, σ) .

Definition 2.21: [8] An IFTS (X, τ) is said to be an Intuitionistic fuzzy $bT_{1/2}$ ($\text{IF}bT_{1/2}$ in short) space if every IFGbCS in X is an IFCS in X .

Definition 2.22: [8] An IFTS (X, τ) is said to be an Intuitionistic fuzzy $bgT_{1/2}$ ($\text{IF}bgT_{1/2}$ in short) space if every IFGbCS in X is an IFGCS in X .

III. INTUITIONISTIC FUZZY GENERALIZED b CONTINUOUS MAPPINGS

In this section we have introduced Intuitionistic fuzzy generalized b continuous mapping and studied some of its properties.

Definition 3.1: A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an Intuitionistic fuzzy generalized semi continuous (IFGb continuous in short) if $f^{-1}(B)$ is an IFGbCS in (X, τ) for every IFCS B of (Y, σ) .

Example 3.2: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.2, 0.3), (0.4, 0.7) \rangle$, $T_2 = \langle y, (0.3, 0.4), (0.7, 0.6) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. Then f is an IFGb continuous mapping.

Theorem 3.3: Every IF continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF continuous mapping. Let A be an IFCS in Y . Since f is IF continuous mapping, $f^{-1}(A)$ is an IFCS in X . Since every IFCS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence f is an IFGb continuous mapping.

Example 3.4: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.3, 0.2), (0.6, 0.7) \rangle$, $T_2 = \langle y, (0.4, 0.3), (0.5, 0.6) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.5, 0.6), (0.4, 0.3) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IFCS in X . Therefore, f is an IFGb continuous mapping but not an IF continuous mapping.

Theorem 3.5: Every IF α continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF α continuous mapping. Let A be an IFCS in Y . Then $f^{-1}(A)$ is an IF α CS in X . Since every IF α CS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence, f is an IFGb continuous mapping.

Example 3.6: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.3, 0.2), (0.6, 0.8) \rangle$, $T_2 = \langle y, (0.3, 0.3), (0.5, 0.6) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.5, 0.6), (0.3, 0.3) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IF α CS in X . Then f is IFGb continuous mapping but not an IF α continuous mapping.

Theorem 3.7: Every IFR continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFR continuous mapping. Let A be an IFCS in Y . Then by hypothesis $f^{-1}(A)$ is an IFRCS in X . Since every IFRCS is an IFbGSCS, $f^{-1}(A)$ is an IFGbCS in X . Hence, f is an IFGb continuous mapping.

Example 3.8: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.2, 0.4), (0.8, 0.6) \rangle$, $T_2 = \langle y, (0.3, 0.5), (0.7, 0.5) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.7, 0.5), (0.3, 0.5) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IFRCS in X . Then f is IFGb continuous mapping but not an IFR continuous mapping.

Theorem 3.9: Every IFGS continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFG continuous mapping. Let A be an IFCS in Y . Then by hypothesis $f^{-1}(A)$ is an

IFGCS in X . Since every IFGCS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence f is an IFGb continuous mapping.

Example 3.10: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.5, 0.6), (0.2, 0.2) \rangle$, $T_2 = \langle y, (0.6, 0.6), (0.3, 0.2) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.3, 0.2), (0.6, 0.6) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IFGSCS in X . Then f is IFGb continuous mapping but not an IFGS continuous mapping.

Theorem 3.11: Every IF α G continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IF α G continuous mapping. Let A be an IFCS in Y . Then, by hypothesis $f^{-1}(A)$ is an IF α GCS in X . Since, every IF α GCS is an IFGSCS and every IFGSCS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence f is an IFGb continuous mapping.

Example 3.12: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.5, 0.5), (0.4, 0.5) \rangle$, $T_2 = \langle y, (0.5, 0.7), (0.5, 3) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.5, 0.3), (0.5, 0.7) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IF α GCS in X . Then f is IFGb continuous mapping but not an IF α G continuous mapping.

Theorem 3.13: Every IFGP continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFWG continuous mapping. Let A be an IFCS in Y . Then, by hypothesis $f^{-1}(A)$ is an IFWGCS in X . Since, every IFWGCS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence, f is an IFGb continuous mapping.

Example 3.14: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $T_1 = \langle x, (0.4, 0.3), (0.6, 0.7) \rangle$, $T_2 = \langle x, (0.6, 0.7), (0.4, 0.3) \rangle$. Then $\tau = \{0\sim, T_1, 1\sim\}$ and $\sigma = \{0\sim, T_2, 1\sim\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.4, 0.3), (0.6, 0.7) \rangle$ is IFCS in Y . Then $f^{-1}(A)$ is IFGbCS in X but not IFGPCS in X . Then, f is IFGb continuous mapping but not an IFGP continuous mapping.

Theorem 3.15: Every IFWG continuous mapping is an IFGb continuous mapping but not conversely.

Proof: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFGP continuous mapping. Let A be an IFCS in Y . Then, by hypothesis $f^{-1}(A)$ is an IFGPCS in X . Since, every IFGPCS is an IFGbCS, $f^{-1}(A)$ is an IFGbCS in X . Hence, f is an IFGb continuous mapping.

Example 3.16: Let $X = \{ a, b \}$, $Y = \{ u, v \}$ and $T_1 = \langle x, (0.2, 0.3), (0.8, 0.7) \rangle$, $T_2 = \langle x, (0.4, 0.5), (0.6, 0.5) \rangle$, $T_3 = \langle y, (0.6, 0.5), (0.4, 0.5) \rangle$. Then $\tau = \{0_-, T_1, T_2, 1_-\}$ and $\sigma = \{ 0_-, T_3, 1_-\}$ are IFTs on X and Y respectively. Define a mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. The IFS $A = \langle y, (0.4, 0.5), (0.6, 0.5) \rangle$ is IFCS in Y. Then $f^{-1}(A)$ is IFGbCS in X but not IFWGCS in X. Then, f is IFGb continuous mapping but not an IFWG continuous mapping.

The relations between various types of Intuitionistic fuzzy continuity are given in the following diagram. In this diagram ‘cts’ means continuous.

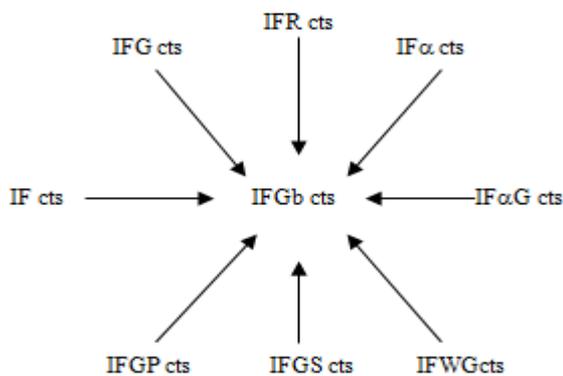


Fig. 1. Relation between Intuitionistic fuzzy generalized b continuous mappings and other existing Intuitionistic fuzzy mappings.

None of them is reversible.

Theorem 3.17: A mapping $f: X \rightarrow Y$ is IFGb continuous then the inverse image of each IFOS in Y is an IF α GOS in X.

Proof: Let A be an IFOS in Y. This implies A^c is IFCS in Y. Since f is IFGb continuous, $f^{-1}(A^c)$ is IFGbCS in X. Since $f^{-1}(A^c) = (f^{-1}(A))^c$, $f^{-1}(A)$ is an IFGbOS in X.

Theorem 3.18: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFGb continuous mapping, then f is an IF continuous mapping if X is an IF $_bT_{1/2}$ space.

Proof: Let A be an IFCS in Y. Then $f^{-1}(A)$ is an IFGbCS in X, since f is an IFGb Continuous. Since X is an IF $_bT_{1/2}$ space, $f^{-1}(A)$ is an IFCS in X. Hence f is an IF continuous mapping.

Theorem 3.19: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFGb continuous function, then f is an IFG continuous mapping if X is an IF $_{gb}T_{1/2}$ space

Proof: Let A be an IFCS in Y. Then $f^{-1}(A)$ is an IFGbCS in X, by hypothesis. Since X is an IF $_{gb}T_{1/2}$ space, $f^{-1}(A)$ is an IFGCS in X. Hence f is an IFG continuous mapping.

Theorem 3.20: Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an IFGb continuous mapping and $g: (Y, \sigma) \rightarrow (Z, \delta)$ is IF continuous, then $g \circ f: (X, \tau) \rightarrow (Z, \delta)$ is an IFGb continuous.

Proof: Let A be an IFCS in Z. Then, $g^{-1}(A)$ is an IFCS in Y, by hypothesis. Since, f is an IFGb continuous mapping, $f^{-1}(g^{-1}(A))$ is an IFGbCS in X. Hence, $g \circ f$ is an IFGb continuous mapping.

IV. CONCLUSION

In this paper we have introduced Intuitionistic fuzzy generalized b continuous mappings and studied some of its basic properties. Also, we have studied the relationship between Intuitionistic fuzzy generalized continuous mappings and some of the Intuitionistic fuzzy continuous mappings already exist.

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